| Course Code | Course Title | L | P | U |
| :---: | :---: | :---: | :---: | :---: |
| MAT123T | Differential Equations I | $\mathbf{4}$ | $\mathbf{0}$ | $\mathbf{4}$ |

## Course Objectives:

To put it briefly, the course objective of the course is to take the existing knowledge of calculus and apply it towards the construction and solution of mathematical models in the form of differential equations (i.e. equations with derivatives in them).

Course Outcomes: After the completion of this course, students will be able to

1. Understand all of the concepts relating to the order and linearity of ODEs, analytic and computational solution methods for ODEs, and the real-world applications of ODEs.
2. Apply the concepts, formulas, and understand the problem-solving procedures to thoroughly investigate relevant physical models.
3. Explain the concepts of solution methods, and related ideas at a fundamental level, as well as how and why we use the solution techniques that we use.
4. Determine the solutions of differential equations with given conditions

## Mapping of Course Outcome(s):

| $\begin{aligned} & \hline \mathrm{PO} / \\ & \mathrm{CO} \end{aligned}$ |  | Program Outcomes |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | PO1 | PO2 | PO3 | PO4 | PO5 | PO6 |
|  | CO1 | S | S |  |  | M | S |
|  | CO 2 | S | S |  |  | M | S |
|  | CO3 | S | S |  |  | M | S |
|  | CO 4 | S | S |  |  | M | S |

L-Low, M-Medium, S-Strong

## Course contents:

## Unit 1 (6 L)

Significance of ordinary differential equation. Geometrical and physical consideration. Formation of differential equation by elimination of arbitrary constant. Meaning of the solution of ordinary differential equation. Concept of linear and non-linear differential equations.

Unit 2 ( 8 L)
Equations of first order and first degree: Statement of existence theorem. Separable, Homogeneous and Exact equation. Condition of exactness, Integrating factor. Rules of finding integrating factor, (statement of relevant results only).

## Unit 3 (9 L)

First order linear equations: Integrating factor (Statement of relevant results only). Equations reducible to first order linear equations (Bernoulli's Equation). Method of variation of parameters.

## Unit 4 (4 L)

Equations of first order but not of first degree. Clairaut's equation. Singular solution.
Applications: Geometric applications, $\omega$-trajectories, Orthogonal trajectories.

## Unit 5 (18 L)

Higher order linear equations with constant co-efficients: Complementary function, Particular Integral. Method of undetermined co-efficients, Symbolic operator D. Method of variation of parameters. Exact Equation. Euler's homogeneous equation and Reduction to an equation of constant coefficients.

## References

[1] An Introductory Course on Ordinary Differential Equation - D. A. Murray.
[2] Differential Equations - S. L. Ross.
[3] Differential Equations - H. T. H. Piaggio.
[4] A Text Book of Ordinary Differential Equations - Kiseleyev, Makarenko \& Krasnov.
[5] Differential Equations with Application \& Programs - S. Balachanda Rao, H. R.
Anuradha.
[6] Text Book of Ordinary Differential Equations (2nd Ed.) - S. G. Deo, V. Lakshmikantham \& V. Raghavendra (Tata McGraw Hill).
[7] An Introduction to Differential Equations - Ghosh \& Maity.
[8] Differential Equations - Chakraborty \& Ghosh.

Lecture-wise plan:

| Lecture No. | Learning objective | Topics to be covered | Reference (Ch./Sec./ Page Nos. of Text Book) |
| :---: | :---: | :---: | :---: |
| 1-6 | To appreciate the connection between general laws of nature and diff. eqns. | Significance of ordinary differential equation. Geometrical and physical consideration | Ref 7 |
|  |  | Formation of differential equation by elimination of arbitrary constant | Ref 7 |
|  |  | Meaning of the solution of ordinary differential equation | Ref 7 |
|  |  | Concept of linear and nonlinear differential equations. | Ref 7 |
| 7-14 | Equations of first order and first degree | Statement of existence theorem | Ref 2 |
|  |  | Variable separable equation | Ref 7 |



## Evaluation Scheme:

| Component | $\underline{\text { Duration }}$ | $\frac{\text { Weightage }}{\underline{(\%)}}$ | $\underline{\text { Remarks }}$ |
| :--- | :---: | :---: | :---: |
| Internal I | To be <br> decided | 25 | Closed Book |
| Mid term | 2 hrs. | 20 | Closed Book |
| Internal II | To be <br> decided | 25 | Closed Book |
| Comprehensive Exam | 3 hrs. | 30 | Closed Book |

1. Attendance Policy: A Student must normally maintain a minimum of $\mathbf{7 5 \%}$ attendance in the course without which he/she shall be disqualified from appearing in the respective examination.
2. Make-up Policy: A student, who misses any component of evaluation for genuine reasons, must immediately approach the instructor with a request for make-up examination stating reasons. The decision of the instructor in all matters of make-up shall be final.
3. Chamber Consultation Hours: During the Chamber Consultation Hours, the students can consult the respective faculty in his/her chamber without prior appointment.
