

# Optimal City Structure

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# Motivation

- ▶ An unprecedented concentration of people in cities:
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- ▶ How to design city policies (infrastructure, incentives, zoning regulations etc)?
  - ▶ **Challenge:** various economic linkages (trade, migration, commuting), agglomeration economies (knowledge spillovers, scale economies), complex geographies
- ▶ Little theory work on city policies in urban models:
  - ▶ Typically difficult to construct equilibrium, let alone design real-life urban policy

# This paper

- ▶ A quantitative GE urban model to evaluate design of city policies
  - ▶ Urban structure with *production spillover links*: quantitative version of Fujita Ogawa/Lucas Rossi-Hansberg, and also *amenity spillover links*
    - ▶ Arbitrary geography, locations separated by time & trade costs.
  - ▶ *Model trade* (Allen Arkolakis '14) & *commuting* (Ahfelt et al) *links* in equilibrium

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- ▶ Generalization of urban models (Rosen-Roback) to analyze “place based” policies
  - ▶ Sharp characterization of equilibrium properties (existence, uniqueness, efficiency)
  - ▶ Straightforward mapping to available spatial micro-data
  - ▶ Equilibrium welfare summarized by single value (the eigenvalue of the system)
    - ▶ Allows to design planner that yields efficient allocations; map it to market results

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- ▶ Zoning: policy that regulates and establishes limits on the use of land/building.
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- ▶ Apply framework to determine the benefit of relaxing zoning regulations and how close Chicago's current zoning to planner's optimum.

# Literature review

- ▶ Model encompasses in one GE framework:
  - ▶ *Trade*: Anderson '79, Eaton Kortum '02, Melitz-Chaney ....
  - ▶ *Geography (Labor mobility)*: Krugman '91, Helpman '98, Redding Sturm '08, Allen Arkolakis '14, Redding '15
  - ▶ *Commuting*:
    - ▶ Fixed utility, no trade links: Ahlfedlt, Redding, Sturm, Wolf '14
    - ▶ Endogenous utility with commuting & trade: Monte, Redding, Rossi-Hansberg '15
  - ▶ *Knowledge externalities & endogenous time allocation*: Glaeser '99, Lucas Rossi-Hansberg '03, Rossi-Hansberg '05, Davis Dingel '13, Ioannides '12
- ▶ Characterizing equilibrium properties of spatial models
  - ▶ Allen Arkolakis '14, Allen Arkolakis Takahashi '14, Allen Arkolakis Li '15
- ▶ Urban economics and regional policies
  - ▶ Baldwin et al '03, Rossi-Hansberg '07, Glaeser Gottlieb '08, Moretti and Kline '14, Turner '14

# Roadmap

- ▶ Theoretical framework
- ▶ Characterizing the equilibrium
- ▶ Optimal (real world) city structure
- ▶ Conclusion

# Outline of the Talk

## Theoretical framework

- Setup

- Gravity of people and goods

## Characterizing the equilibrium

- Aggregation

- Equilibrium

- Model Properties

- Social Planner and Welfare

## Optimal (real world) city structure

- Data

- Identification

- Optimal City Structure

## Conclusion

## Setup: Geography

- ▶ Locations in the city:  $\Theta = \{1, 2, \dots, N\}$ 
  - ▶ each location endowed with  $H_i$  units of buildings ( $i \in \Theta$ ).
  - ▶ buildings can be used in residential ( $H_{Ri}$ ) or commercial use ( $H_{Fi}$ ) with

$$H_{Ri} + H_{Fi} \leq H_i.$$

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- ▶ Two types of areas:
  - ▶ Residential area:  $\Theta_R = \{i | i \in \Theta, H_{Ri} > 0\}$
  - ▶ Commercial area:  $\Theta_F = \{i | i \in \Theta, H_{Fi} > 0\}$
  - ▶ The following cases are allowed
    - ▶ Mixed use:  $\Theta_R \cap \Theta_F \neq \emptyset$
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- ▶ Locations  $(i, j)$  separated by :
  - ▶ Iceberg trade costs  $\tau_{ij} \geq 1$  ( goods)
  - ▶ Travel time costs,  $d_{ij} \geq 0$  ( people)

## Setup: Production

- ▶ Each location produces differentiated variety
- ▶ Cobb-Douglas production function

$$Y_i = A_i L_{Ei}^\alpha H_{Fi}^{1-\alpha},$$

where  $A_i$  is productivity,  $L_{Ei}$  is the number of effective labor.

- ▶ Firms in each location are perfectly competitive, so we have wage and rent:

$$w_i = \alpha p_i L_{Ei}^{\alpha-1} H_{Fi}^{1-\alpha},$$

$$r_{Fi} = (1 - \alpha) p_i L_{Ei}^\alpha H_{Fi}^{-\alpha}$$

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- ▶ Agent has one unit of time, which is allocated between commuting  $d_{ij}$  and working  $t_{ij} = 1 - d_{ij}$ .
- ▶ Agent needs to decide where to live, where to work and the consumption over housing and goods.

# Agent's Problem

- ▶ Agent maximizes utility in each step

$$\max_{i \in \Theta_R} \mathbb{E} \left[ \max_{j \in \Theta_F} \max_{h_i(\omega), Q_i(\omega)} u_j h_i(\omega)^{1-\beta} Q_i(\omega)^\beta \right]$$

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- ▶ Second, knowing him/her own productivity, agent chooses where to work in  $j \in \Theta_F$ .
- ▶ Last, knowing above information, agent determines the consumption.

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subject to  $\sum_{k \in \Theta_F} p_{ki} q_{ki}(\omega) + r_{Ri} h_i(\omega) \leq e_j(\omega)$  where

$$Q_i(\omega) = \left( \sum_k q_{ki}(\omega)^{\frac{\sigma-1}{\sigma}} \right)^{\sigma/(\sigma-1)}.$$

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- ▶ Second, maximize indirect utility,

$$\max_{j \in \Theta_F} c \frac{e_j(\omega)}{P_i^\beta r_{Ri}^{1-\beta}}$$

where  $e_j(\omega) = y^c + w_j a_j(\omega) t_{ij}$ ,  $y^c$  is capital income,  $a_j(\omega)$  is realized productivity,  $\{a_j(\omega)\}$  follows a i.i.d. Frechet distribution across all  $j \in \Theta_F$ .

- ▶ Last, maximize expected utility,

$$\max_{i \in \Theta_R} u_i \frac{y^c + \Gamma \left( \frac{\theta-1}{\theta} \right) W_i}{P_i^\beta r_{Ri}^{1-\beta}}$$

where  $W_i = \left( \sum_j (w_j t_{ij})^\theta \right)^{\frac{1}{\theta}}$ .

# Macro Implications of Agent's Decision

- ▶ Gravity of goods

$$X_{ij} = \frac{p_i^{1-\sigma} \tau_{ij}^{1-\sigma}}{P_j^{1-\sigma}} \beta E_j,$$

where  $P_j = \left( \sum_i p_i^{1-\sigma} \tau_{ij}^{1-\sigma} \right)^{1/(1-\sigma)}$ , is the CES price index

- ▶ Gravity of commuting

$$L_{ij} = \frac{(w_j t_{ij})^\theta}{W_i^\theta} L_{Ri},$$

where  $W_i = \left( \sum_j (w_j t_{ij})^\theta \right)^{\frac{1}{\theta}}$ , is the ex-ante expected wage

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## Conclusion

# Aggregation on trade and commuting

## ▶ Aggregation on Commercial Area Side

- ▶ (Goods) Production Balance

$$Y_i = \sum_j X_{ij},$$

- ▶ (People) Aggregation of effective labor accounting:

$$L_{Ej} = \sum_i l_{ij} L_{ij}$$

where  $l_{ij} = \Gamma \left( \frac{\theta-1}{\theta} \right) \frac{W_i}{w_j t_{ij}} t_{ij}$ .

## ▶ Aggregation on Residential Area Side

- ▶ (Goods) Budget Balance (Price Index):

$$\beta E_i = \sum_j X_{ji}$$

- ▶ (People) Commuting balance

$$L_{Ri} = \sum_j L_{ij}$$

# Aggregation of spillovers

## ▶ Spatial Spillovers:

- ▶ Productivity Spillover

$$A_i = \bar{A}_i \left( \sum_j K_{ij}^A L_{Ej} \right)^\eta$$

- ▶ Amenity

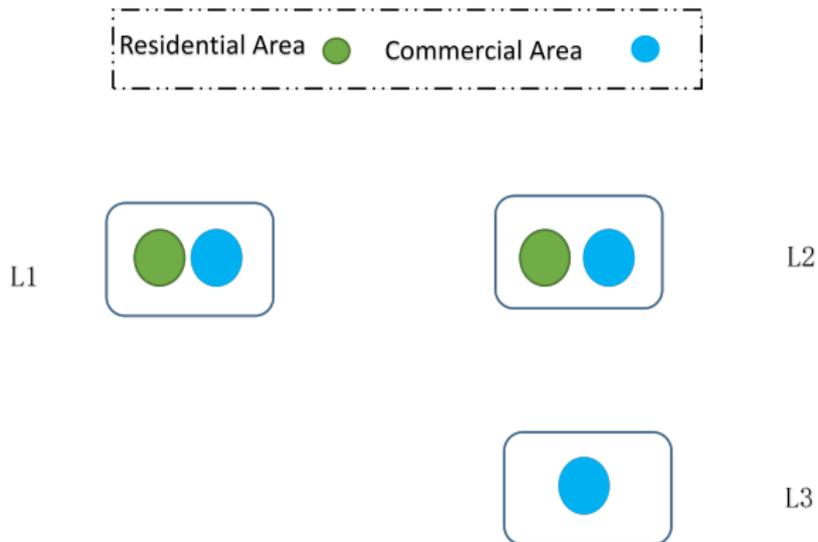
$$u_i = \bar{u}_i \left( \sum_j K_{ij}^u L_{Rj} \right)^\epsilon$$

## ▶ Welfare Equalization

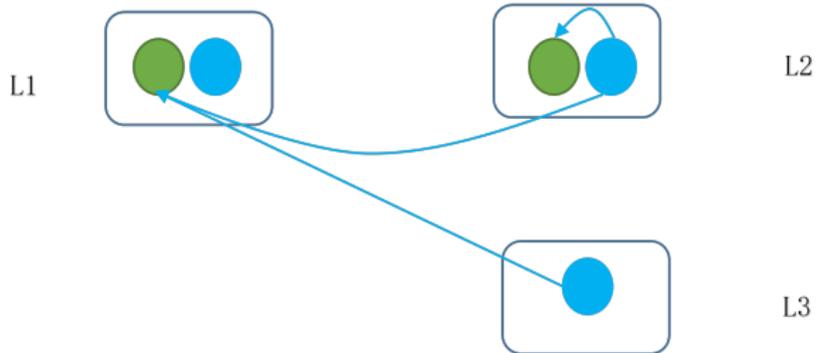
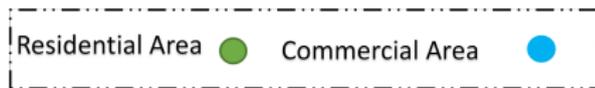
$$W = \frac{u_i e_i}{P_i^\beta r_{Ri}^{1-\beta}}$$

where  $e_i = y^c + \Gamma \left( \frac{\theta-1}{\theta} \right) W_i$ .

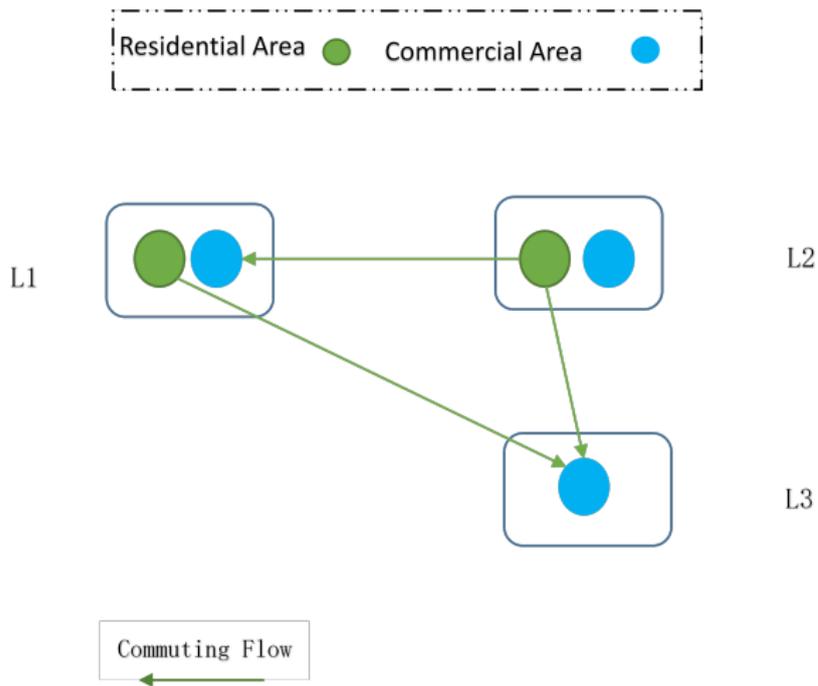
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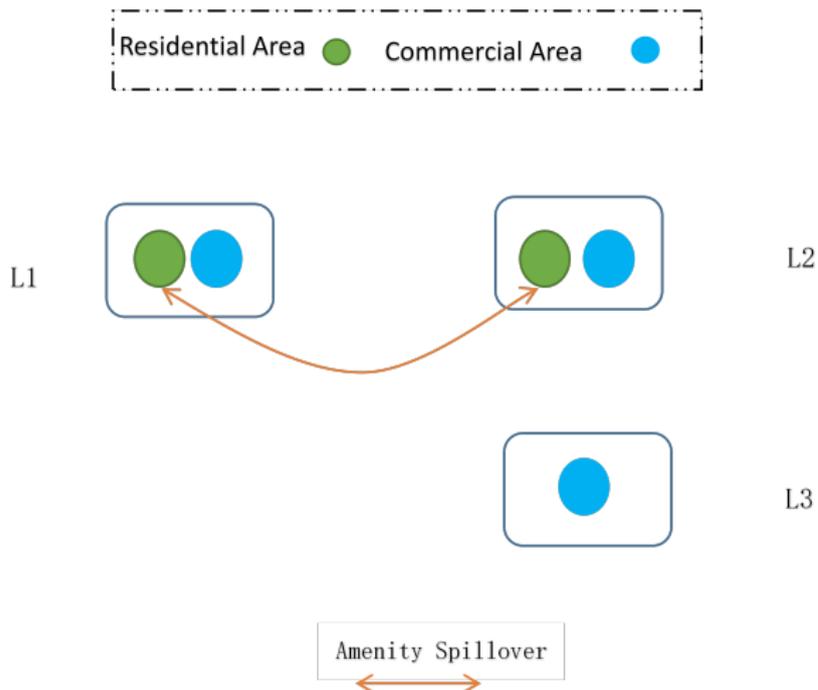
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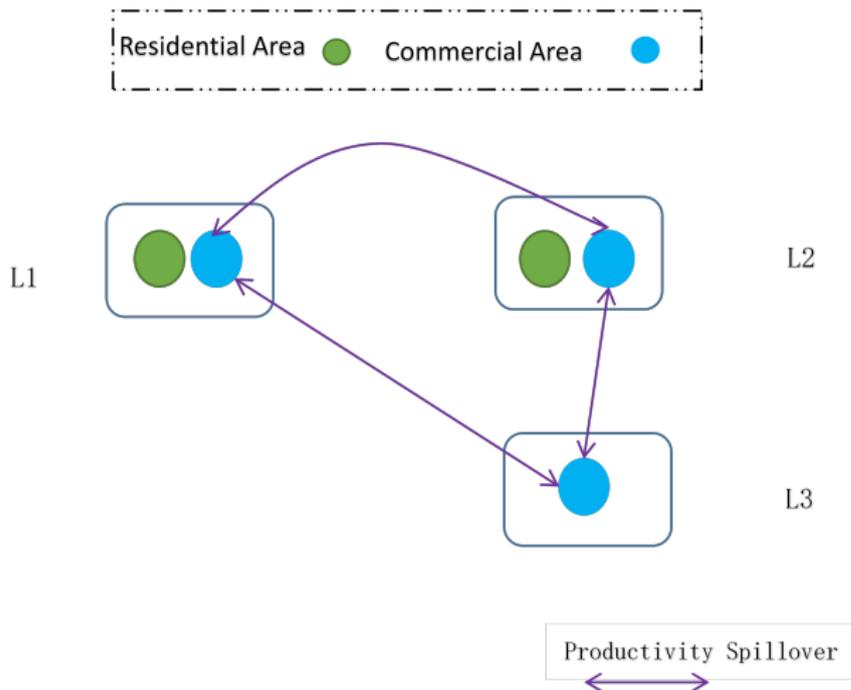
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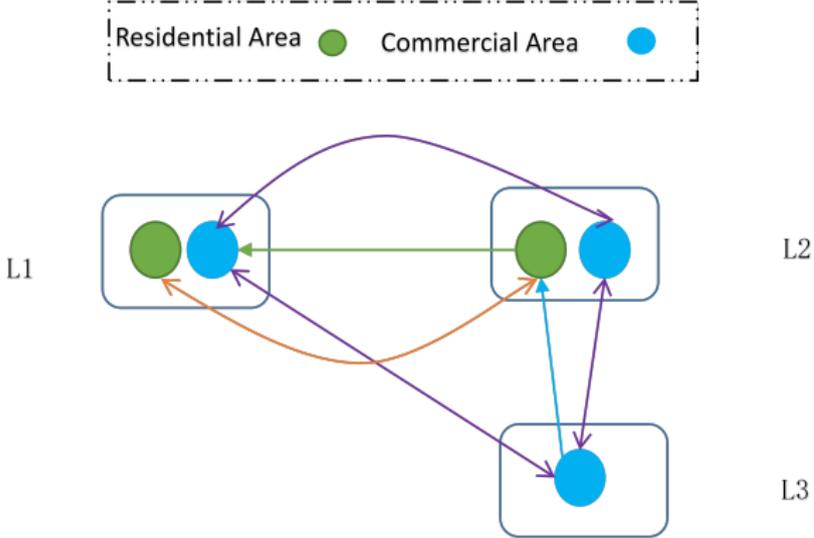
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## Market Equilibrium vs. zoning

- ▶ **Zoning Equilibrium** (denoted as  $\mathcal{F}_1$ ) is characterized by equilibrium equations on commercial area, residential area, spatial spillover equation and welfare equalization condition. In Zoning Equilibrium,  $\{H_{Ri}, H_{Fi}\}$  are exogenously given.

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- ▶ **Market Equilibrium without zoning** ( $\mathcal{F}_2$ ),  $\mathcal{F}_1$  and  $\{H_i^F\}$  and  $\{H_i^R\}$  determined by rent equalization:

$$\begin{cases} r_{Ri} = r_{Fi} & \text{if } H_{Ri} > 0 \\ H_{Ri} = 0 & \text{if } W > \frac{u_i e_i}{P_i^\beta r_{Fi}^{1-\beta}} \end{cases}$$

▶ 
$$H_i = H_{Fi} + H_{Ri} \quad \forall i \in \{1, \dots, N\}.$$

# Existence and uniqueness

## Theorem

*(Existence and Uniqueness) Consider the above Zoning Equilibrium  $\mathcal{F}_1$ ,*

*i) An equilibrium solution always exists.*

*ii) If trade costs are zero, the equilibrium is unique (for prices variables, it is up-to-scale unique) if the following inequalities are satisfied,*

$$|\eta| \leq \frac{\alpha(\sigma - 1)(1 - \theta) + \sigma\theta}{(\sigma - 1)|\theta - 1|},$$

$$|\epsilon| \leq \frac{1 - \beta}{\beta},$$

and

$$g(|\epsilon|, |\eta|) \leq 0$$

where  $g(|\epsilon|, |\eta|)$  increases with  $|\epsilon|$  and  $|\eta|$ .

► Implication on policy:

- multiple equilibria when spatial spillover strengths are strong.

## Equilibrium Characterization: no trade costs and symmetry

- ▶ In general, analytical solutions of the equilibrium do not exist.
- ▶ In certain special cases, however, they do: Assume that  $\alpha = \beta = 1$  (no land rents) and assume no trade costs
  - ▶ We can write equilibrium as

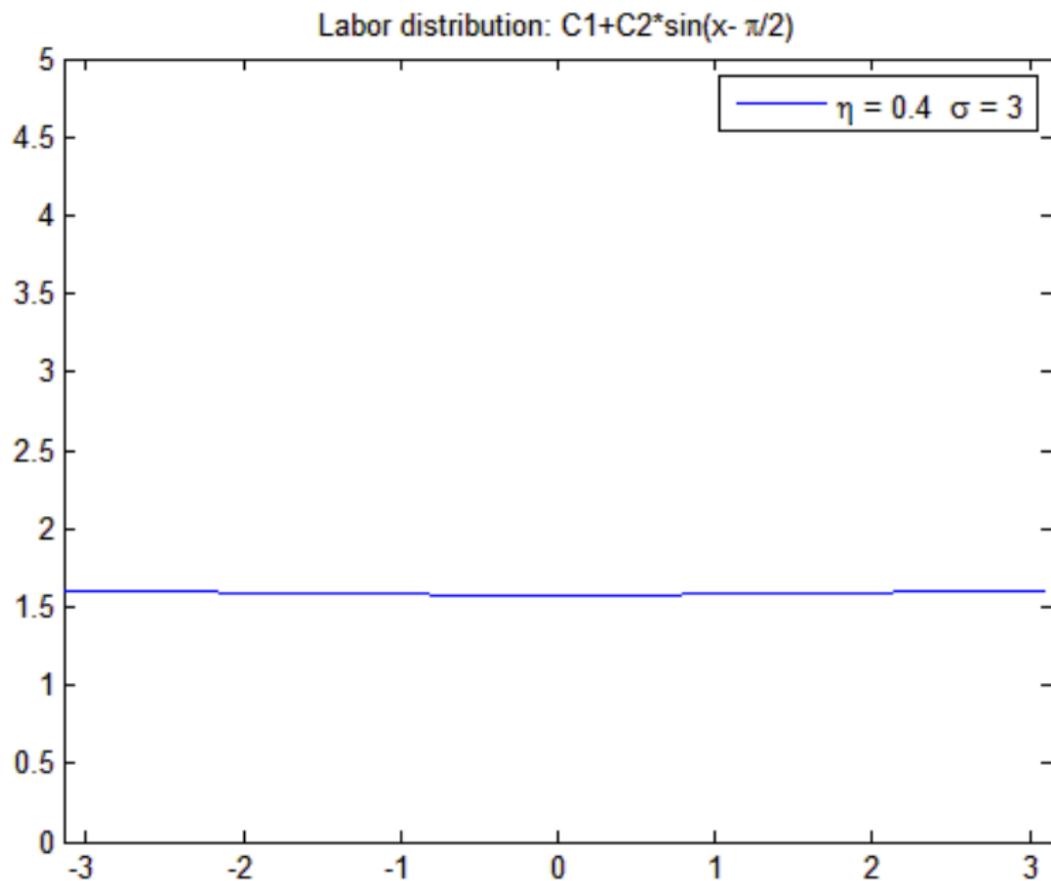
$$\left(L_i^E\right)^{\sigma_1 \tilde{\epsilon}} = \left(\frac{\bar{L}}{W^\theta} \beta^{\frac{\theta}{\sigma}} E^{\frac{\theta}{\sigma}}\right)^{\frac{1}{1+\theta}} \sum_j \tilde{K}_{ij}^A \left(L_j^E\right)^{\eta \tilde{\epsilon}}$$

- ▶ Consider now the geography of a circle,  $S = [-\pi, \pi]$ 
  - ▶ Also assume exogenous productivities, amenities and land is symmetric
  - ▶ And that  $\tilde{K}_{ij}^A = C \left[\cos\left(\frac{i-j}{2}\right)\right]^2$
- ▶ System attains a solution

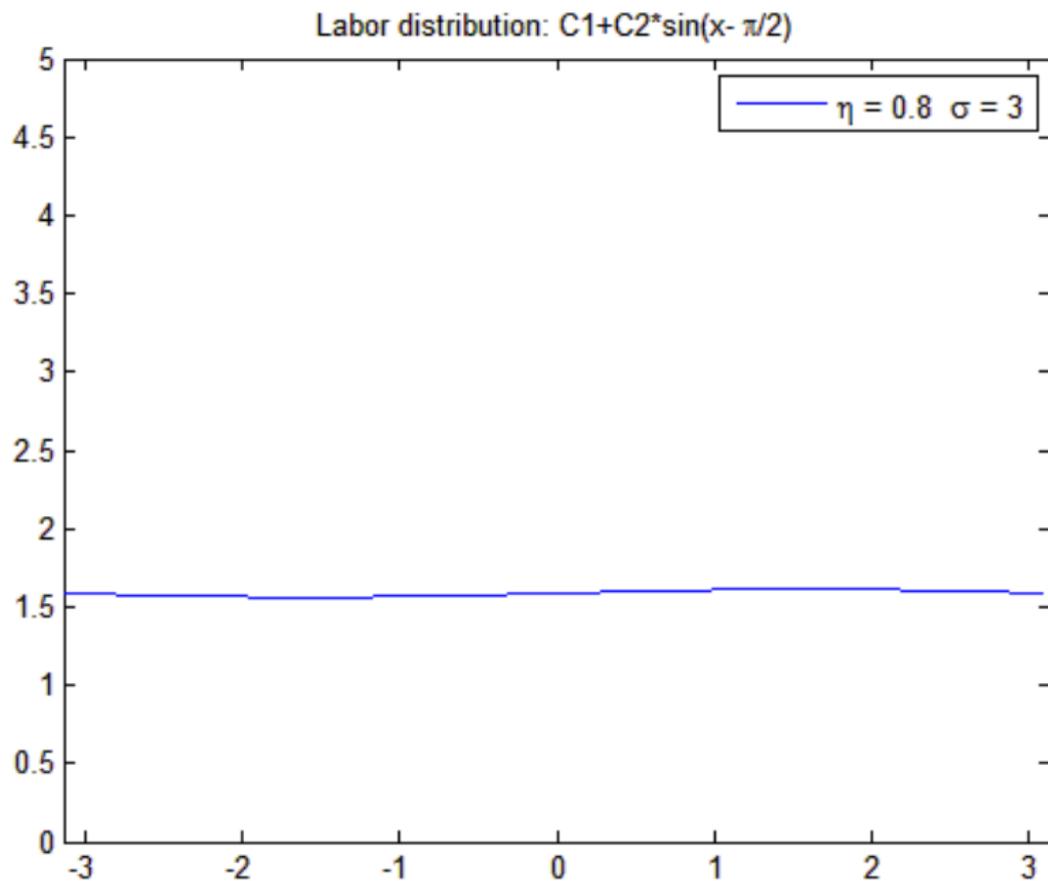
$$\left(L_i^E\right)^{\sigma_1 \tilde{\epsilon}} = Y + \sqrt{Y^2 + C_1} \sin(i + C_2)$$

where  $Y^2 + C_1 \geq 0$ , and  $C_2$  is arbitrary due to symmetry.

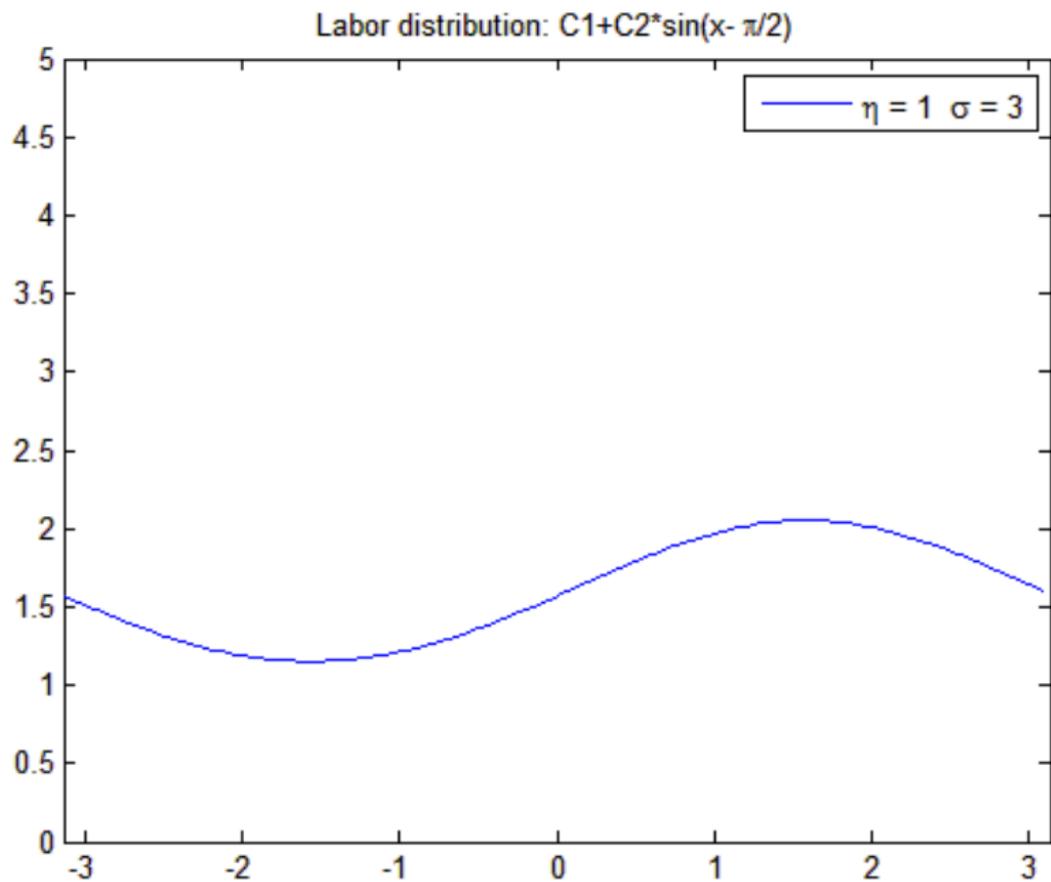
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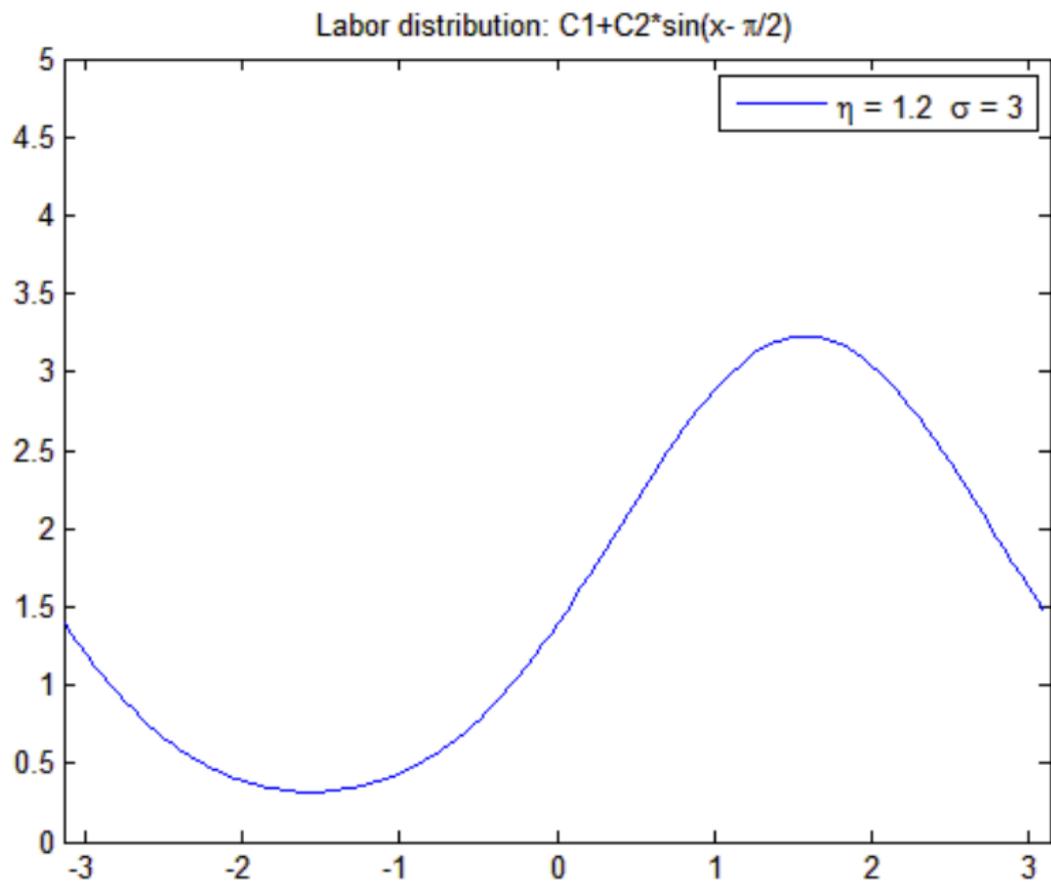
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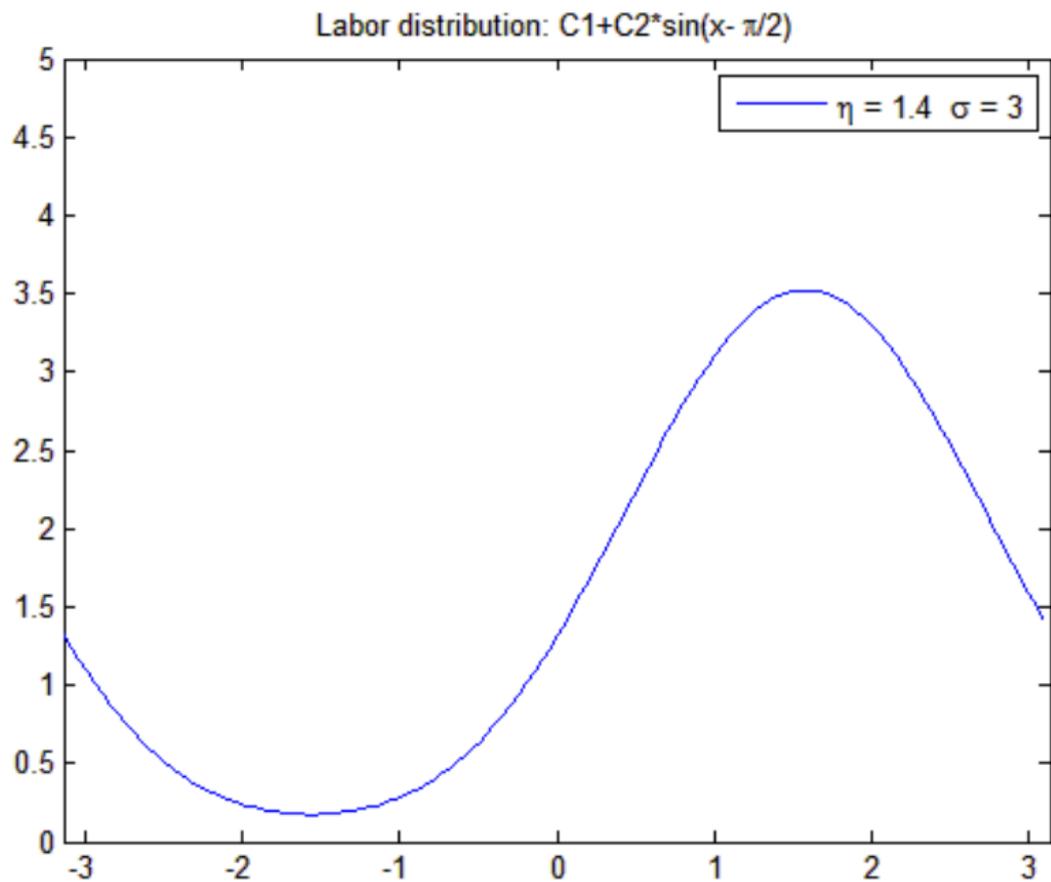
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## The Planner and the role for zoning

- ▶ Zoning Social Planner,  $S^Z$ , is social planner who maximizes  $W$

$$\max_{\{H_{Fi}, H_{Ri}\}_{i \in \Theta}} W$$

subject to

$$H_i = H_{Fi} + H_{Ri}$$

and the zoning equilibrium  $\mathcal{F}_1$ .

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*(iii) (preliminary) There exists a set of (Pigovian) taxes on labor such that the market equilibrium  $\mathcal{F}_2$  achieves at least as high social welfare function as the solution to the Ramsey problem, i.e. zoning is a “second best” policy instrument.*

# The welfare effect of zoning

## Proposition

*Suppose we observe global parameters,  $\kappa = \theta, \alpha, \beta, \sigma, \eta, \epsilon$ , data matrices on bilateral flows of goods and people  $\pi$ . Then:*

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2. **(Local counterfactual)** For any observed equilibrium, the elasticity of welfare for small changes in  $H_{Ri}$  or  $H_{Fi}$  can be expressed as a function of  $\kappa, \pi$  alone:

$$\frac{d \ln W}{d \ln H_{Ri}} = G^R(\kappa, \pi) \quad \text{and} \quad \frac{d \ln W}{d \ln H_{Fi}} = G^F(\kappa, \pi)$$

where  $G^R(\kappa, \pi)$  and  $G^F(\kappa, \pi)^H$  are closed form expressions (see paper).

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3. **(Necessary optimality condition)** At the optimal zoning, following FOCs hold for  $H_{Ri} > 0$ :

$$\frac{d \ln W}{d \ln H_{Fi}} \frac{1}{H_{Fi}} = \frac{d \ln W}{d \ln H_{Ri}} \frac{1}{H_{Ri}}$$

# Outline of the Talk

## Theoretical framework

- Setup

- Gravity of people and goods

## Characterizing the equilibrium

- Aggregation

- Equilibrium

- Model Properties

- Social Planner and Welfare

## Optimal (real world) city structure

- Data

- Identification

- Optimal City Structure

## Conclusion

# Data

- ▶ As an example, focus on Chicago.

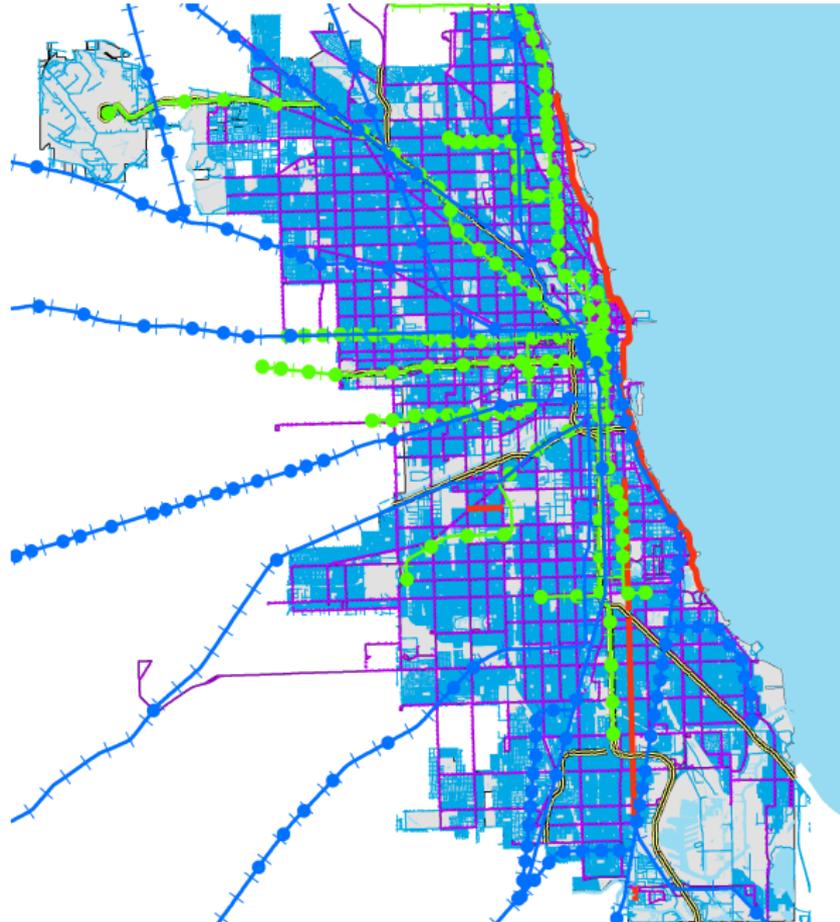
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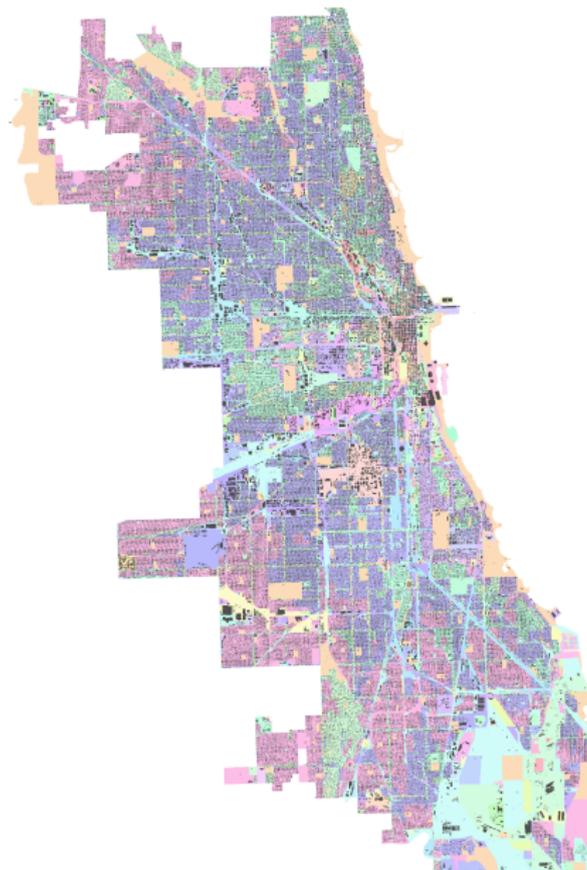
# Transportation infrastructure



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  - ▶ Use FMM to calculate travel time between any two census block groups by either private or public transportation (cross-check with Google Maps).
- ▶ For all  $\sim 820,000$  buildings:
  - ▶ Zoning of building.
  - ▶ Square footage / # of stories.
  - ▶ Can construct  $H_{Fi}$  and  $H_{Ri}$ .

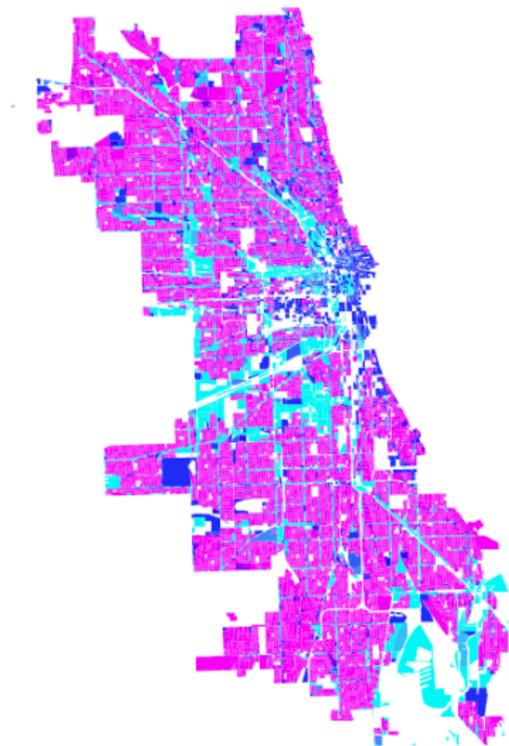
# Buildings and Zoning



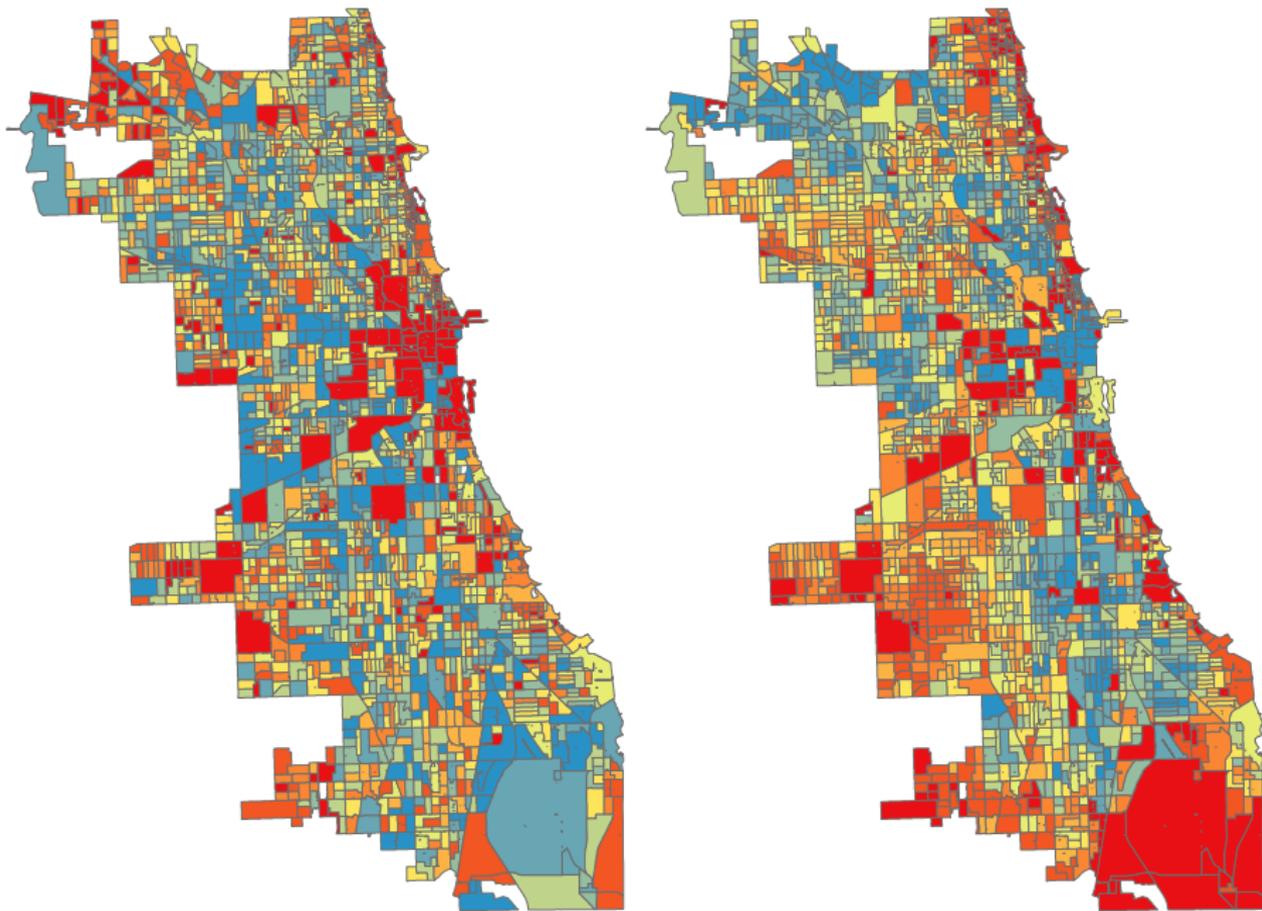
# Buildings and Zoning (CBD)



## Buildings m<sup>2</sup> and Fraction Residential



# Estimated composite productivities ( $A_i$ ) and amenities ( $u_i$ )



# Optimal City Structure in Chicago

- ▶ To determine optimal (local) city structure in Chicago, we apply the results from Proposition 1.
  - ▶ Current results preliminary based on different rent redistribution (proportional to wage)

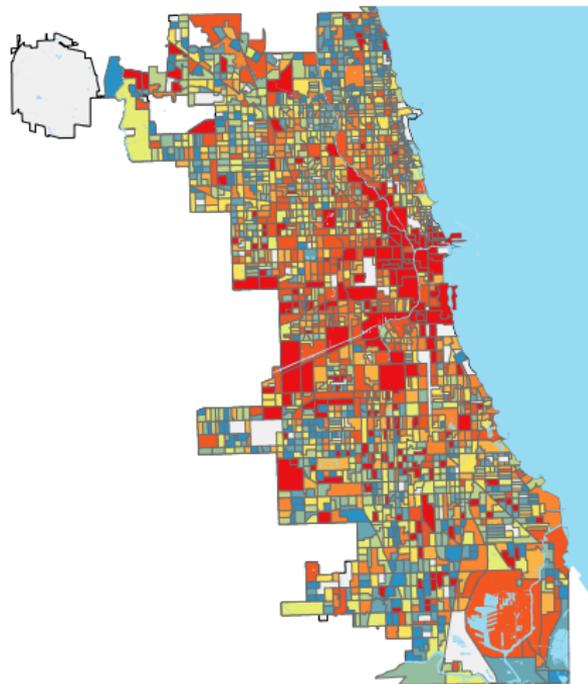
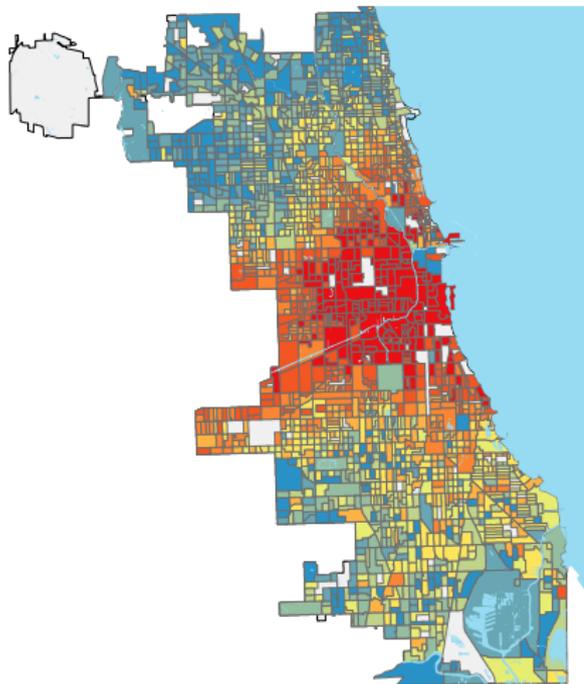
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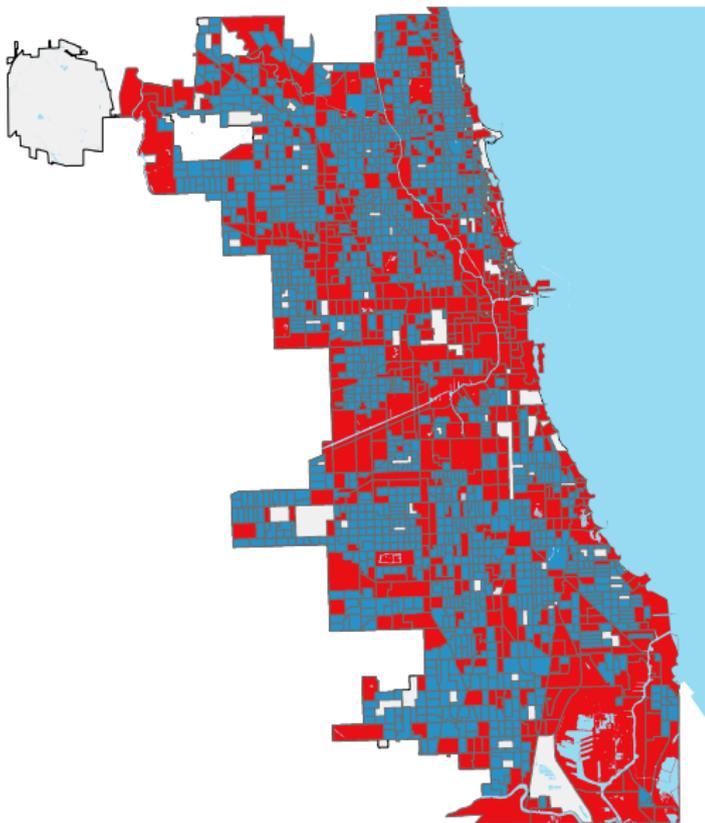
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- ▶ Two exercises (effect of implementing policy on  $i$  for  $W$ ):
  - ▶ Relax building regulations: calculate elasticity of welfare to increasing total area by increasing commercial ( $\frac{d \ln W}{d \ln H_{Fi}}$ ) or residential area ( $\frac{d \ln W}{d \ln H_{Ri}}$ ) using part (ii) of Proposition 1.
  - ▶ Reallocate zoning: reallocate more area to residential (which occurs  $\iff$   $\frac{d \ln W}{d \ln H_{Ri}} \frac{1}{H_{Ri}} > \frac{\partial \ln W}{\partial \ln H_{Fi}} \frac{1}{H_{Fi}}$ ).

Estimated elasticity of city welfare to increasing commercial  $\left(\frac{\partial \ln W}{\partial \ln H_{Fi}}\right)$  and residential area  $\left(\frac{d \ln W}{d \ln H_{Ri}}\right)$



Reallocate area: residential (red) or commercial (blue)?



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  - ▶ Incorporate a number of the spatial linkages present in cities.
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- ▶ Broader scheme of things:
  - ▶ Develop a set of mathematical tools to characterize properties of GE models with spatial interactions.