Variations Practice Exercises III

For each of the following, combine the given sequence of variations into a single variation. Write your answer in the form T_n , T_nR , T_nI , or T_nIR , where $0 \le n \le 11$.

- 1. $RT_4RT_4RT_8$
- 2. *T*₃*IRIT*₈
- 3. $T_5 IRT_7 IRT_8$

Solutions appear on the following page...

Solutions

1. $RT_4RT_4RT_8$

Remember that transpositions and retrogrades commute – that is, you can interchange them without affecting the result. So, using the rules presented in class (and also in the text), we can proceed as follows:

$$\underbrace{RT_4}_{T_4R} RT_4 \underbrace{RT_8}_{T_8R} = T_4 \underbrace{RR}_{T_0} \underbrace{T_4T_8}_{T_0} R = T_4 R$$

Note that we can "cancel" the two consecutive retrogrades (RR); similarly, T_4 and T_8 are opposites, so they "cancel" as well.

2. *IT*₃*IRIT*₈

For #2 and #3, there are inversions, so we have to be a bit more careful about simplifying expressions. Don't forget the rule for interchanging inversions and transpositions: $IT_n = T_{12-n}I$...

$$\underbrace{IT_3}_{T_9I}IR\underbrace{IT_8}_{T_4I} = T_9\underbrace{II}_{T_0}\underbrace{RT_4}_{T_4R}I = \underbrace{T_9T_4}_{T_1}\underbrace{RI}_{IR} = T_1IR$$

Note that at the last step above, T_9T_4 combine to give us T_{13} ; we then apply our "mod 12" rule to replace T_{13} with T_1 .

3.
$$T_5 I \underset{T_7 R}{RT_7} I \underset{T_8 R}{RT_8} = T_5 \underset{T_5 I}{IT_7} R \underset{T_4 I}{IT_8} R = T_5 T_5 I \underset{T_4 R}{RT_4} \underset{RI}{RI} = \underbrace{T_5 T_5}_{T_10} \underbrace{I T_4}_{T_8 I} \underset{T_0}{R} R = \underbrace{T_{10} T_8}_{T_6} \underbrace{II}_{T_0} = T_6$$