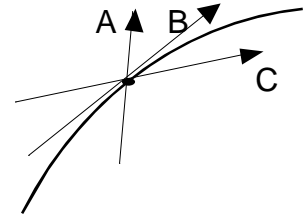


1. The curved line in the diagram at the right represents the path of a moving object. The dot on that path represents the location of the object at a certain time. At an earlier time the object was on the curve somewhere to the left of that dot, and later it is on the curve someplace to the right.



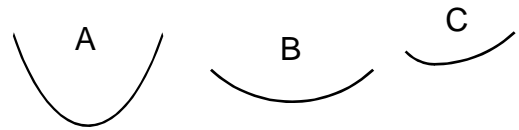
- a. The object's *velocity* can be described by an arrow through that dot.

Which arrow correctly describes the object's velocity? ____

(Remember that the object moves *along* the curve, as in 7b on page 29.)

- b. Whenever an object moves along a curved path, its velocity is _____ to the curve. (See RS II.)

2. One of the curves at the right *could* be the path of a swinging pendulum bob. If the string does not stretch, the path must be a _____ arc, like the one labelled ____.



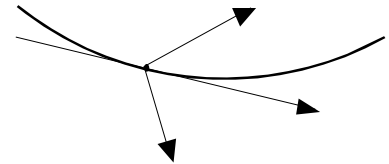
- a. The speed of the bob ____ creases whenever it is moving in a downhill direction, and ____ creases whenever it is going uphill.

- b. The speed of the bob is neither increasing nor decreasing when the bob is at the _____ point of its path. *Please label that point on the bob's path sketched above.*

3. Which arrow in the diagram at the right describes the velocity of a pendulum bob just *before* it reaches the lowest point of its path?

Label it "V₁". The other arrows are wrong because they are

not _____ to the curved path, as in 1b.



4. Draw a large arc on the back of this paper to represent the path of a swinging pendulum bob.

Label the lowest point of the arc. Then make dots on the arc just before and just after that point.

- a. When the bob is passing through dot 1 (just before reaching the midpoint) its velocity is ____ creasing because it is coasting *downhill*. When it passes through dot 2, just *after* passing through the midpoint, its velocity is ____ creasing because it is coasting _____.

- b. Draw arrows through those dots (as in #1) to represent the velocity of the bob as it passes through them. Label the arrows "V₁" and V₂" respectively.

- c. If the second dot on the curve were *higher* than the first dot, then the new velocity would be _____ than the old velocity. If the second dot were *lower*, then V₂ would be _____ than V₁. (more, less)

- d. The second dot is really supposed to be at the *same* altitude as the first one, so the lengths of the two velocity arrows should be _____. *Please adjust them if necessary.*

5. Imagine that the V₁ arrow in #4 is a clock hand. If the "12 o'clock" direction is upward (toward the top of the paper) and the "3 o'clock" direction is eastward, then V₁ is approximately in the ____ o'clock direction, and V₂ is roughly toward ____ o'clock. (Actually, #4 says it must be *less* steep.)

- a. The 12-o'clock direction is upward, the 3-o'clock direction is eastward, and the 9-o'clock direction is ____ ward. The 2 o'clock direction is ____ degrees ____ from east.

- b. The direction *opposite* to 2 o'clock is ____ o'clock, or ____ degrees ____ from _____. An arrow equal but opposite to V₁ would be roughly in the ____ o'clock direction, but _____ steep. (more, less) *Draw* such an arrow in the space at the right. Label it "-V₁".

- c. Starting at the tip (point) of that arrow, draw and label an exact copy of the "V₂" arrow. (Remember that it points roughly in the ____ o'clock direction, but is _____ steeply tilted.)

- d. According to 4c, the lengths of those two arrows must be _____, (equal, unequal) and the absolute values of their slopes must be _____. *Please adjust them if necessary.*

- e. Draw a dotted arrow from the tail of -V₁ to the head of V₂. It represents the *vector sum* of -V₁ and _____. In other words, it describes the object's "_____ in _____", as in 2b on page 41. *Label it.*

- f. If we divide that Δv by Δt (as in 2f on page 41) we see that the bob's acceleration was _____ ward.

6. The **total force** on an object is the *vector sum of all the forces acting on it*. According to 4b on RS III the quotient in 5f is an ____ ward vector *because* the total force on the object is ____ ward. Does that theory agree with the observation you recorded in #4 on RS IV? ____ If not, which is wrong? ____

1. Vector *addition* was reviewed in #5 on page 34R. Here is a similar example involving *subtraction*: Suppose I can paddle a canoe at 8.0 mph relative to the water. When I point the canoe eastward in a river and paddle normally I move relative to the ground at 10 mph, 37 degrees north from east.
 - a. I know that $V_{cg} = \underline{\hspace{1cm}} + \underline{\hspace{1cm}}$. Solving for the unknown, I get $V_{wg} = \underline{\hspace{1cm}} - \underline{\hspace{1cm}}$.
 - b. A negative velocity of 8.0 mph eastward is equivalent to a *positive* velocity of 8.0 mph $\underline{\hspace{1cm}}$ ward, because reversing the *sign* of a vector is equivalent to reversing its $\underline{\hspace{2cm}}$. (clue for 3b)
 - c. Reversing the direction of a relative velocity vector is also equivalent to $\underline{\hspace{2cm}}$ ing its subscripts. For example, if V_{cw} is 8.0 mph eastward, then V_{wc} must be 8.0 mph $\underline{\hspace{1cm}}$ ward.
 - d. It would have been *incorrect* to reverse the vector called " V_{cg} " in this example because in equation 1a there is no $\underline{\hspace{1cm}}$ tive sign in front of the V_{cg} in that equation.
 - e. According to 1a-c, subtracting V_{cw} from V_{cg} is the same as *adding* $\underline{\hspace{1cm}} + \underline{\hspace{1cm}}$.
 - f. Use graphical vector addition (as on 34R) to determine and describe the water's velocity relative to the ground. Make your triangle big enough to get $\pm 1\%$ precision or better. (Use #12 on RS III.)
 - g. Label each arrow clearly (using 1e) and describe the the resultant as on page 34R.

2. Suppose the price of an item was \$10 yesterday and it is \$11 today: Its *change* in price was $\underline{\hspace{1cm}}$ dollars. That change is calculated by $\underline{\hspace{2cm}}$ ing the $\underline{\hspace{1cm}}$ price from the $\underline{\hspace{1cm}}$ price. (new, old) $\underline{\hspace{1cm}} - \underline{\hspace{1cm}} = \underline{\hspace{1cm}}$

3. Suppose my velocity changes from 10 m/sec east to 10 m/sec north during a 2.0-second time interval.
 - a. If I *added* those two velocities, I would get 14.1 m/sec *northeast*. But to find the **CHANGE** in velocity I must $\underline{\hspace{2cm}}$ the $\underline{\hspace{1cm}}$ velocity from the $\underline{\hspace{1cm}}$ velocity. *Does #2 agree?* $\underline{\hspace{1cm}}$
 - * b. Using that plan, describe the magnitude and direction of my change in velocity. Label each of the three arrows clearly, using the symbols V_1 , V_2 , and ΔV . *One of them must have a negative sign.*
 - * c. We know that the "speed" of an object is the magnitude of its velocity. Is it correct to say that the *magnitude of the change in velocity* found in 3b is equal to the corresponding *change in speed*? Please give evidence to support your answer.

4. Suppose you are flying an airplane with a velocity " V_{pa} " relative to the air while the air is moving with a velocity " V_{ag} " relative to the ground. In flier's jargon, V_{ag} is called the "wind velocity", the magnitude of V_{pa} is the plane's "airspeed". Let " V_{pg} " represent the velocity of the plane relative to the ground. The magnitude of V_{pg} is called the aircraft's "groundspeed".
 - a. Using #14 on RS II, how can V_{pg} be determined from the other two velocities? $\underline{\hspace{2cm}}$
 - b. Is the resulting vector diagram necessarily a right triangle? $\underline{\hspace{2cm}}$
 - * c. The wind velocity is learned from weather reports, and V_{pg} is determined from the location of your destination and your intended flying time. How can you use that information (with #1) to decide which way to point the plane and what airspeed to choose to reach the destination on schedule?

5. Suppose you intend to fly 100 miles south relative to the ground in 51 minutes. The wind is "45 mph out of the northeast". That means the air is moving southwest at 45 mph relative to the ground, or that the ground is moving $\underline{\hspace{2cm}}$ at 45 mph relative to the $\underline{\hspace{1cm}}$, as in 1c.
 - a. Describe your planned displacement relative to the ground: $\underline{\hspace{2cm}}$
 - b. Describe your planned average *velocity* relative to the ground: $V_{pg} = \underline{\hspace{1cm}}$ mph $\underline{\hspace{1cm}}$
 - c. According to #4, you can get V_{pa} by subtracting $\underline{\hspace{1cm}}$ from $\underline{\hspace{1cm}}$, or by *adding* $\underline{\hspace{1cm}} + \underline{\hspace{1cm}}$.
 - d. Do that on the back of this paper, striving for $\pm 1\%$ precision. Show your method clearly. If you use a scale drawing then *describe its scale*. Then record the result here, using #2 on p. 34R.

$$V_{pa} = \underline{\hspace{1cm}} \text{ mph , } \underline{\hspace{1cm}} \text{ degrees } \underline{\hspace{1cm}} \text{ from } \underline{\hspace{1cm}}.$$
 - e. Use a protractor to measure each angle in the triangle. Record the results clearly on the diagram. Then use a ruler to measure each side of the triangle, and write those lengths (in cm.) on the arrows.
 - f. Multiply each of those lengths by the scale factor that you recorded in 5d, in *mph per cm*. Record those results on the diagram also. Make sure that 5d agrees with them.